

Denmark Australia Diophantine Approximation Day 2017

Aarhus University, December 8, 2017 organised by Simon Kristensen and Fabien Pazuki, with the support of the Niels Bohr Professorship of Lars Hesselholt.



Program

	Friday 8.12
09:30-10:30	Michael Coons
10:45-11:45	Fabien Pazuki
11:45-13:30	Lunch
13:30-14:30	Evgeniy Zorin
14:45-15:45	Alex Ghitza
15:45-16:30	Coffee break
16:30-17:30	Simon Kristensen
18:30	Dinner

Abstracts

Time: Friday 8, 9:30-10:30.

Room: Aud D1.

Speaker: Michael Coons (Univ. Newcastle, Australia).

Title: 2-automatic sequences, Lyapunov exponents and a dynamical analogue of Lehmer's Mahler measure problem.

Abstract: We show that the Mahler measure of every height-one polynomial can be expressed as the maximal Lyapunov exponent of a matrix cocycle that arises in the spectral theory of 2automatic sequences. In this way, one comes up with a sort of dynamical analogue of Lehmer's problem on minimal Mahler measures. This is joint work with Michael Baake and Neil Manibo (University of Bielefeld, Germany).

Time: Friday 8, 10:45-11:45.

Room: Aud D1.

Speaker: Fabien Pazuki (Univ. Copenhagen, Denmark).

Title: *Elliptic curves and isogenies.*

Abstract: Two elliptic curves E and E' defined over a number field K are isomorphic over the algebraic closure of K if and only if they have the same j-invariant. A natural question is: how is this invariant transformed by general isogenies? We prove a new height bound on the difference of heights of the j-invariants of isogenous elliptic curves, and derive several consequences, for instance bounds for the height of modular polynomials and for Vélu's formulas. If time permits, we will add a remark on Mordell-Weil ranks of elliptic curves.

Time: Friday 8, 13:30-14:30.

Room: Aud D1.

Speaker: Evgeniy Zorin (Univ. York, UK).

Title: Diophantine approximations to automatic numbers.

Abstract: There exists a deep interplay between Diophantine properties of real numbers and computational complexity of their *b*-adic expansions, for any integer $b \ge 2$, or also their continued fractions. I am going to present this area of research and discuss in particular details my recent results, joint with Badziahin (University of Sydney), on Diophantine exponents of automatic numbers.

Time: Friday 8, 14:45-15:45.

Room: Aud D1.

Speaker: Alex Ghitza (Univ. Melbourne, Australia).

Title: Numerical evaluation of Hecke eigenvalues.

Abstract: I will discuss the efficient computation of eigenvalues for the Hecke operators acting on spaces of modular forms. This is a problem that has attracted lots of attention and, lately, lots of heavy algebraic-geometric machinery. In contrast, I wish to describe an elementary, simple-minded numerical-analytic method and discuss its performance for various types of modular forms. Time: Friday 8, 16:30-17:30.

Room: Aud D1.

Speaker: Simon Kristensen (Aarhus Univ., Denmark).

Title: Irrationality of series via uniform distribution.

Abstract: Building on a method of Schlage–Puchta, we investigate the use of uniform distribution theory in proofs of the irrationality of real numbers represented by series. We describe a general method for proving irrationality via uniform distribution and give some (hopefully new) applications. This is joint work in progress with Jaroslav Hancl.